

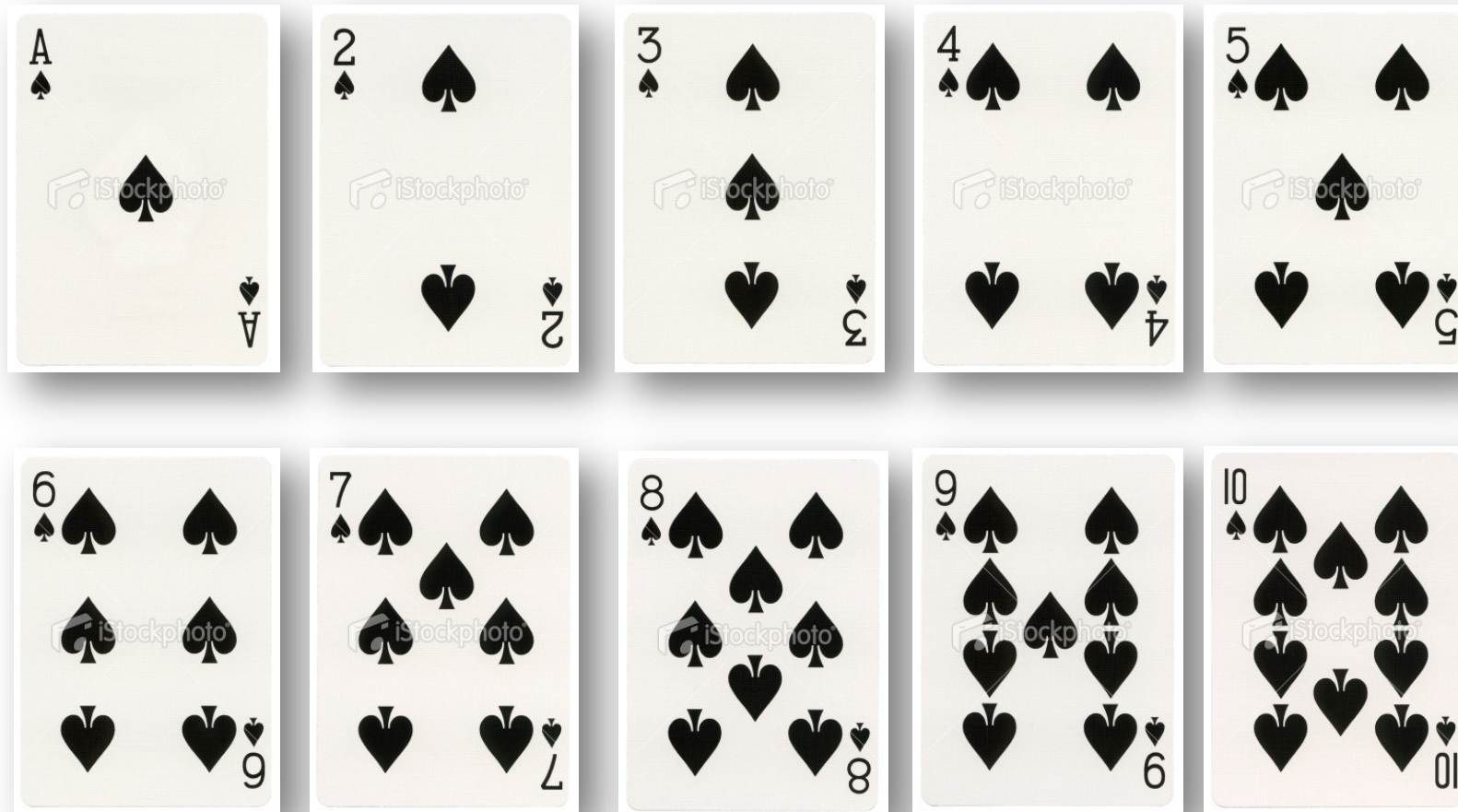
# One-Pass Data stream

Danupon Nanongkai

## Part 1

Warm-up: Finding a missing number

# There are 10 cards: A, 2, 3, ..., 10



# There are 10 cards: A, 2, 3, ..., 10

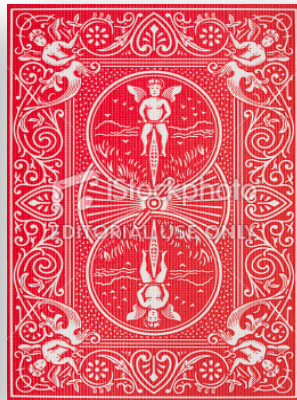
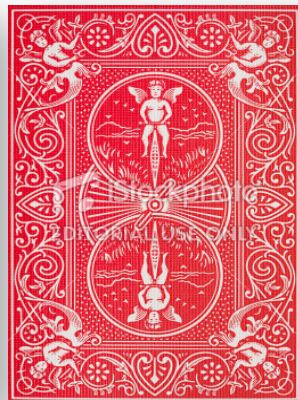
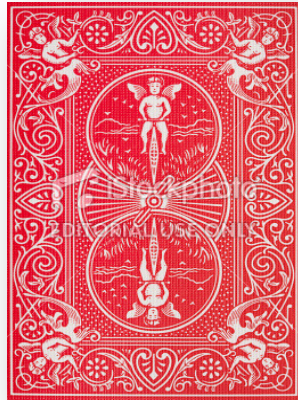
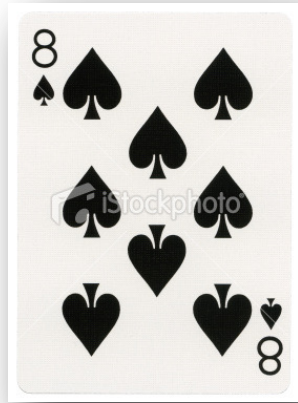




# What is the removed card?

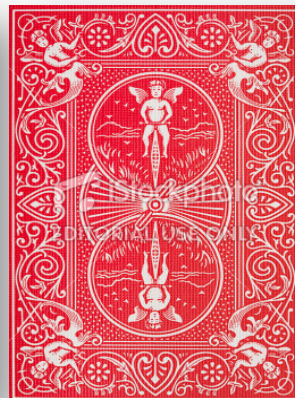
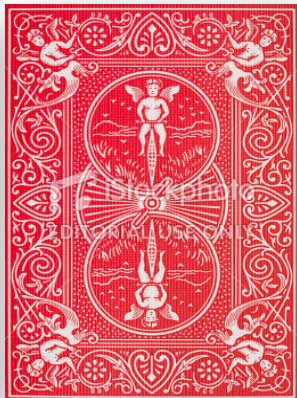
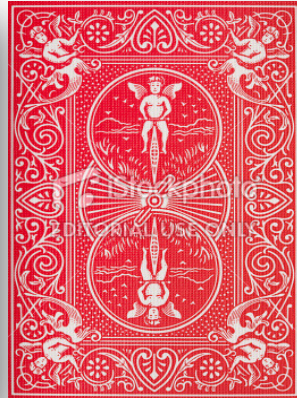
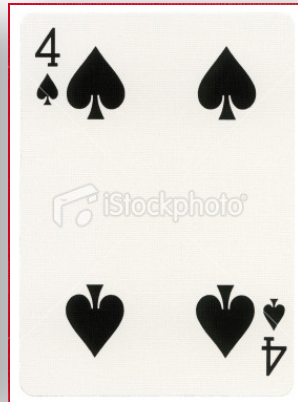
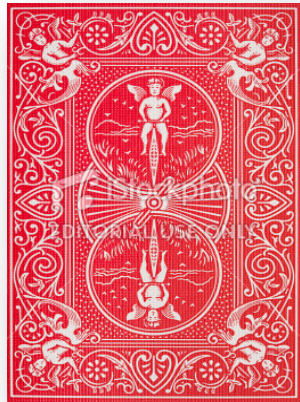


# I will show you one number at a time

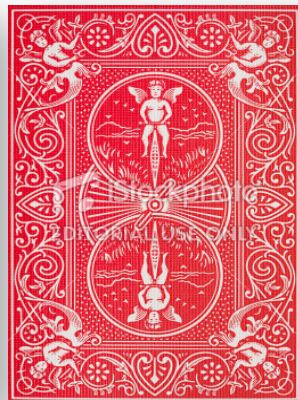
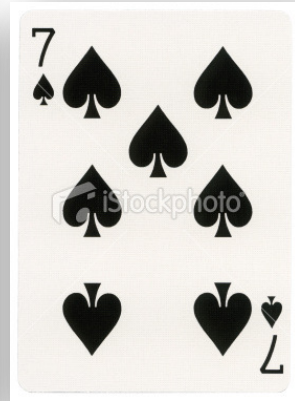




# I will show you one number at a time

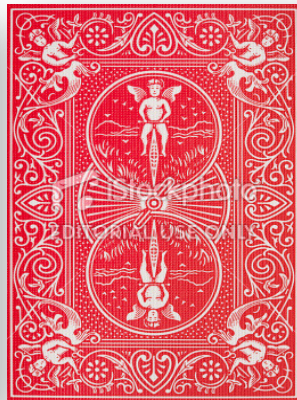
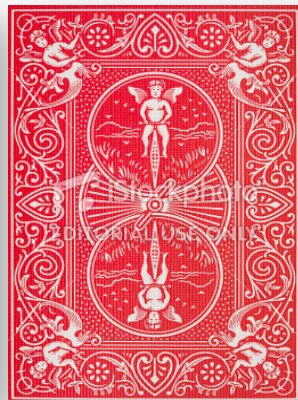
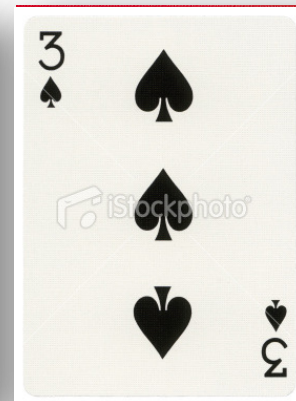


# I will show you one number at a time

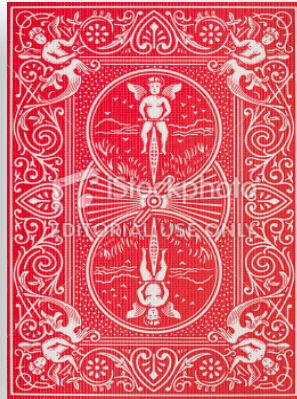
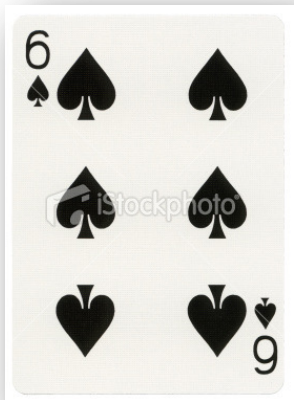
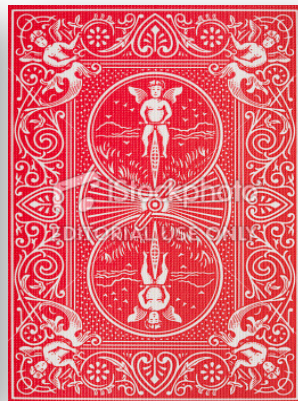




# I will show you one number at a time

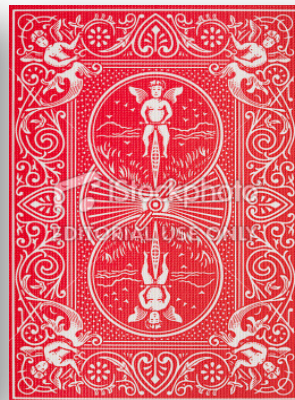
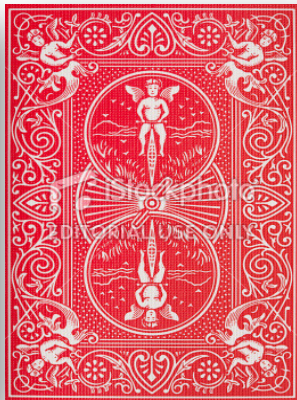
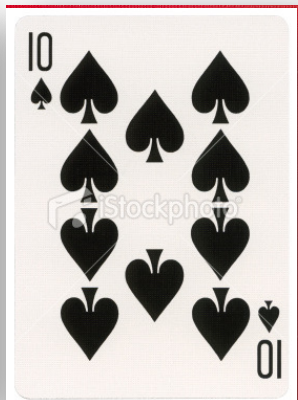
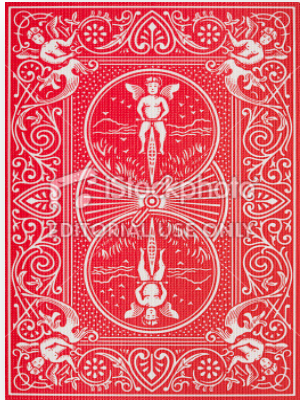
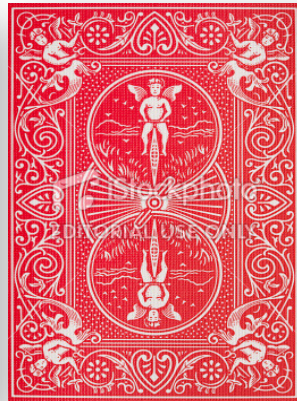
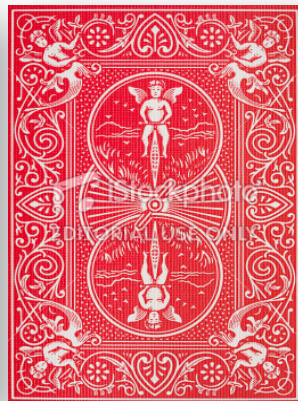


# I will show you one number at a time



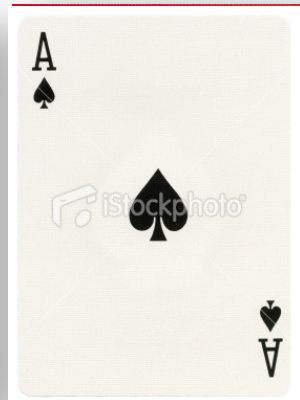
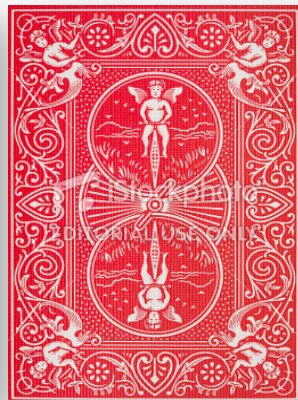


# I will show you one number at a time





# I will show you one number at a time

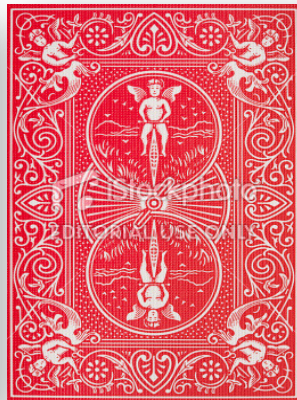
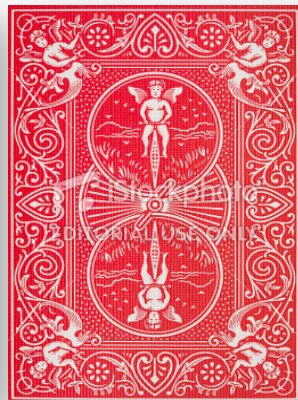


# I will show you one number at a time





# I will show you one number at a time

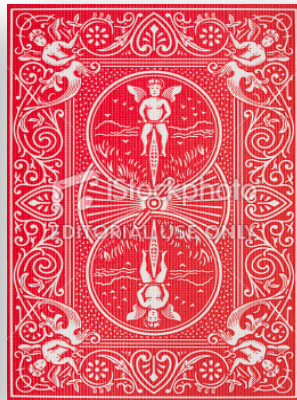
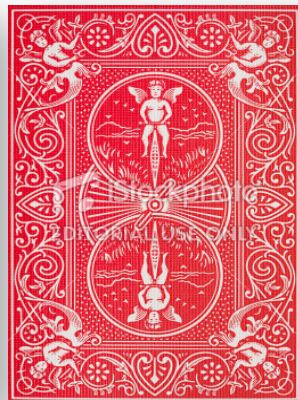
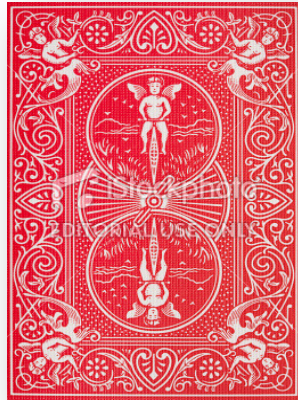
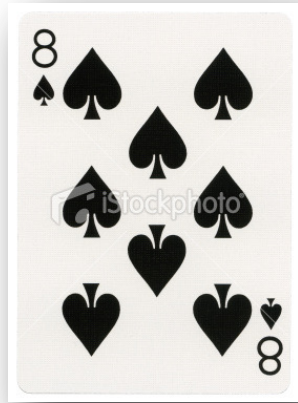




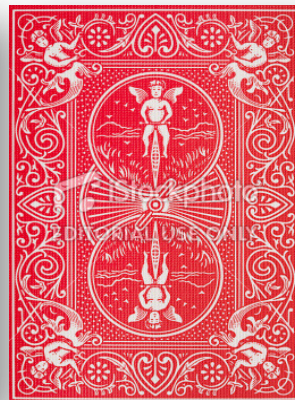
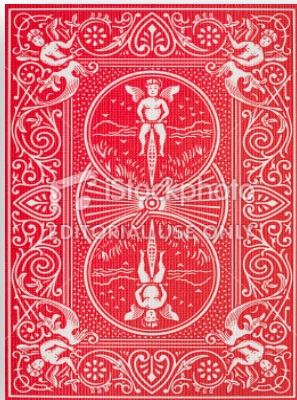
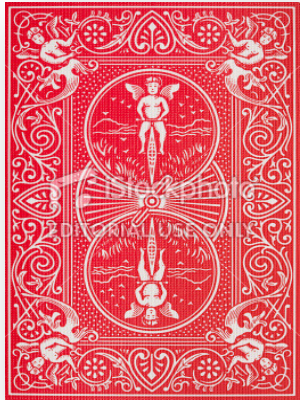
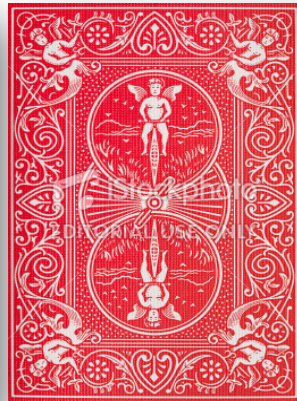
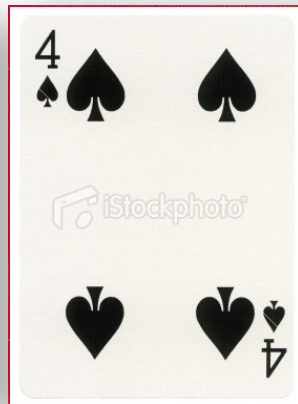
# Let's try again

- Hint: It is enough to just memorize one number

# I will show you one number at a time

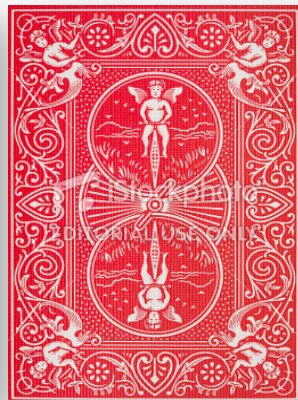
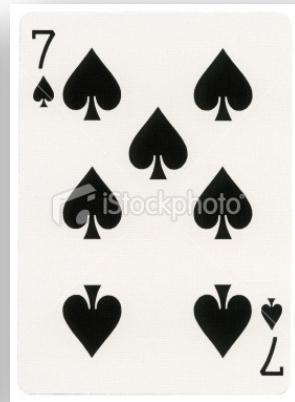


# I will show you one number at a time

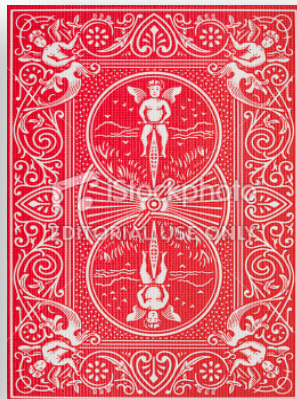
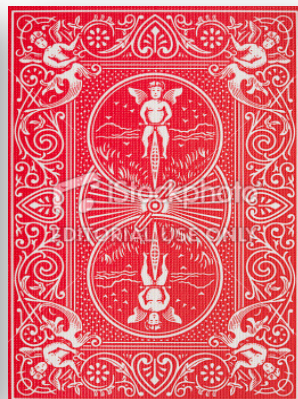
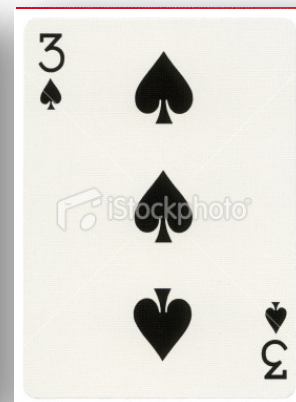
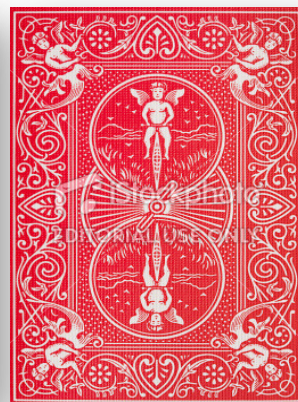
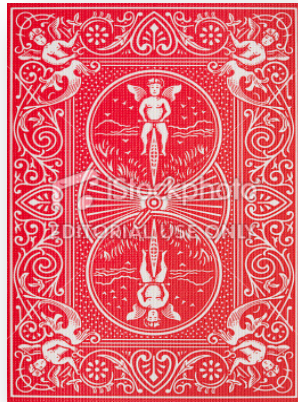




# I will show you one number at a time

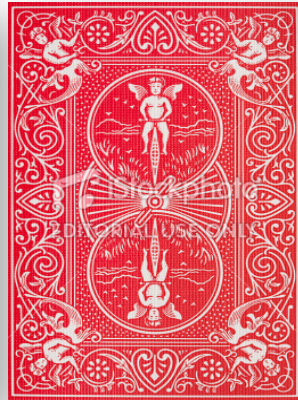
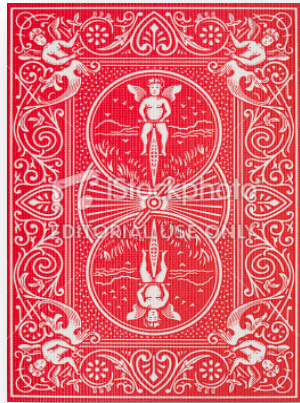


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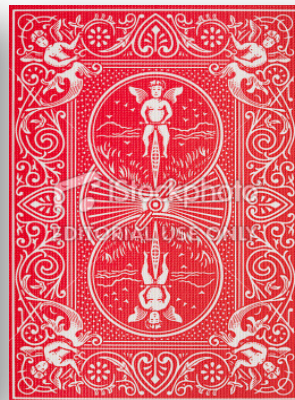
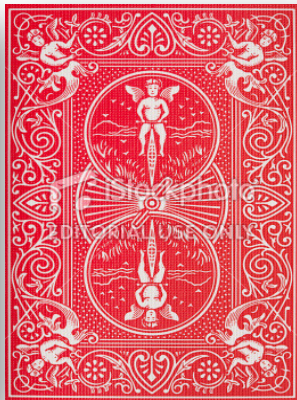
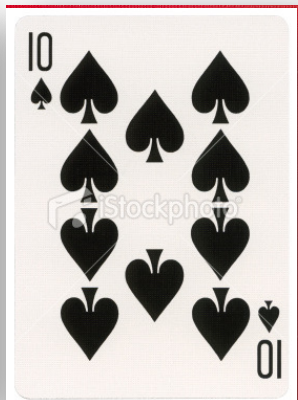
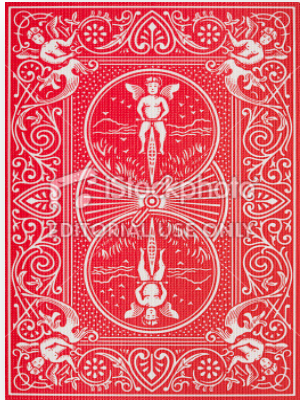
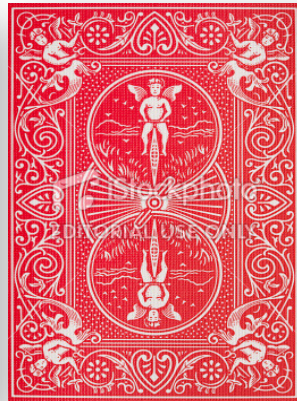
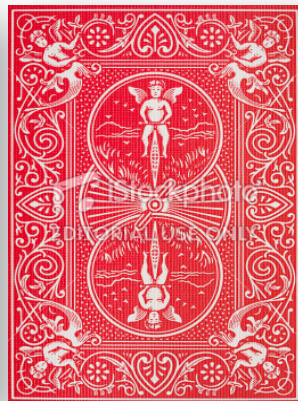


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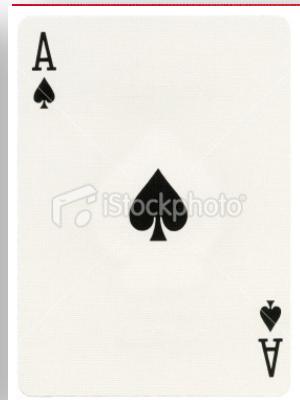
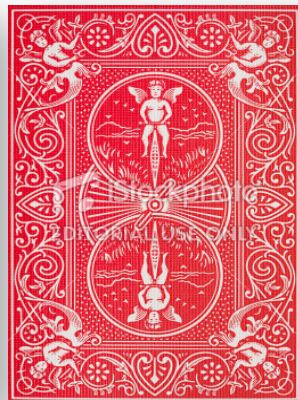




# I will show you one number at a time



# I will show you one number at a time

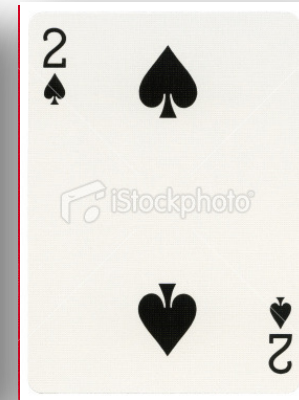
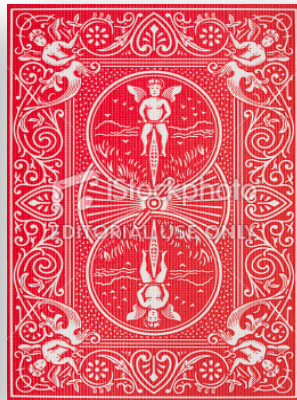
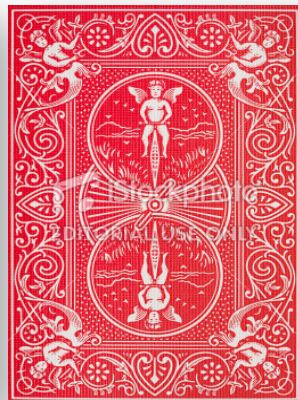




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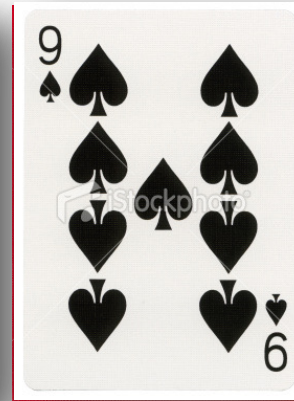
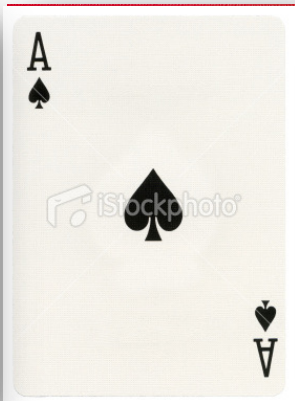
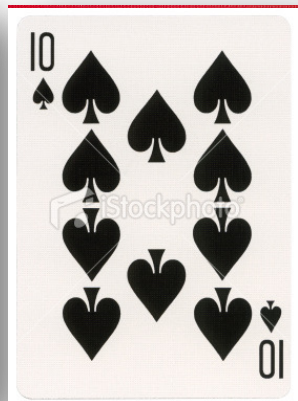
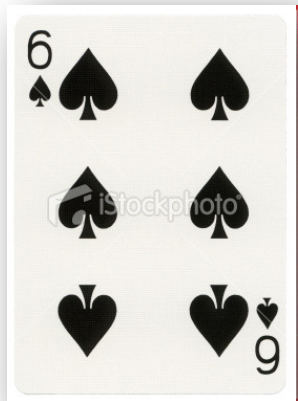
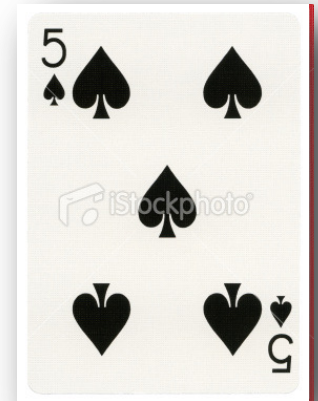
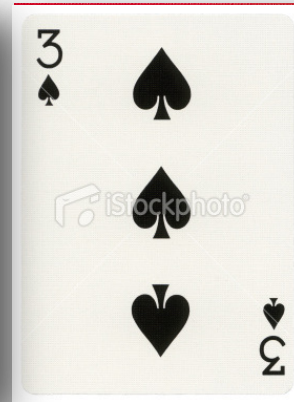
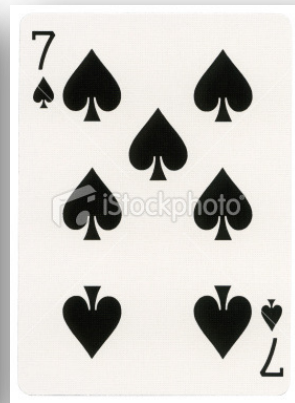
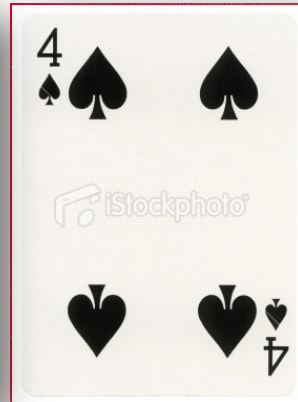
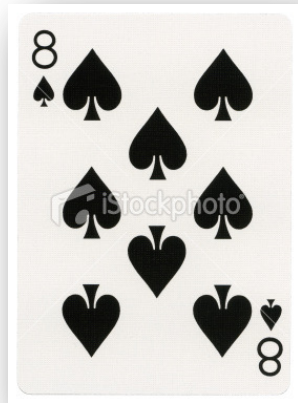


# I will show you one number at a time





Answer



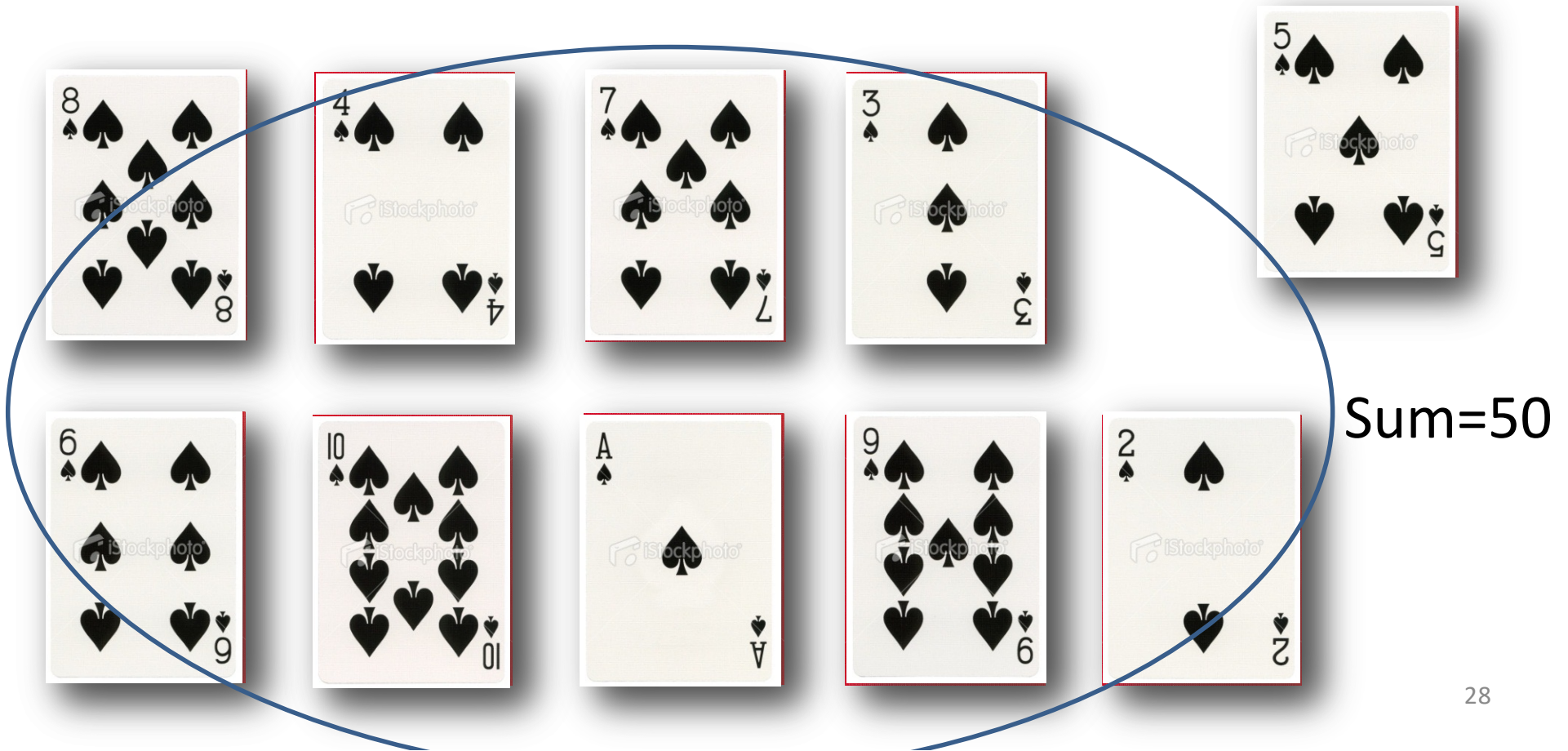


# Algorithm

- Memorize the sum of all numbers
- $1+2+3+\dots+10 = 55$

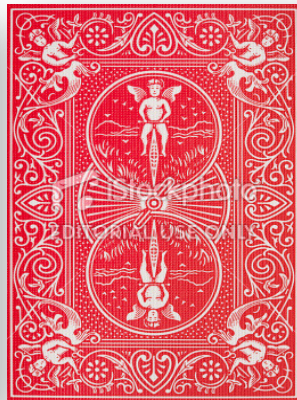
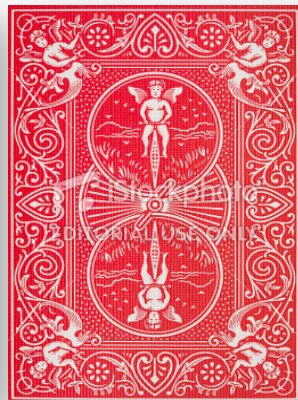
# Algorithm

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- $1+2+3+\dots+10 = 55$

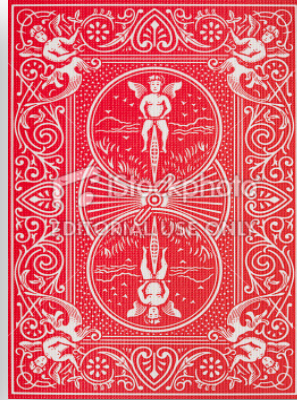
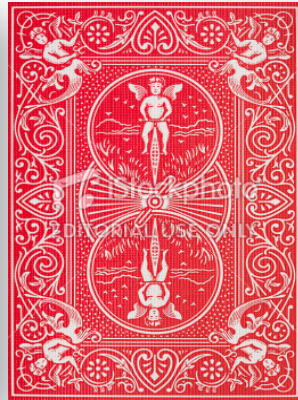
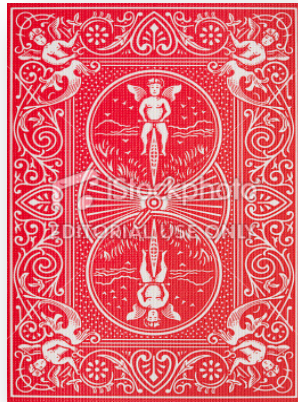




# What are the removed cards?



# What are the removed cards?





Remove **x** cards  $\rightarrow$  remember **x** numbers

# Data Stream Model



# Data Stream Model



1 3 5 9 2 10 11 12 20



Small memory

# Data Stream Model



1 3 5 9 2 10 11 12 20



Small memory



# Data Stream Model



1 3 **5** 9 2 10 11 12 20



Small memory

# Data Stream Model



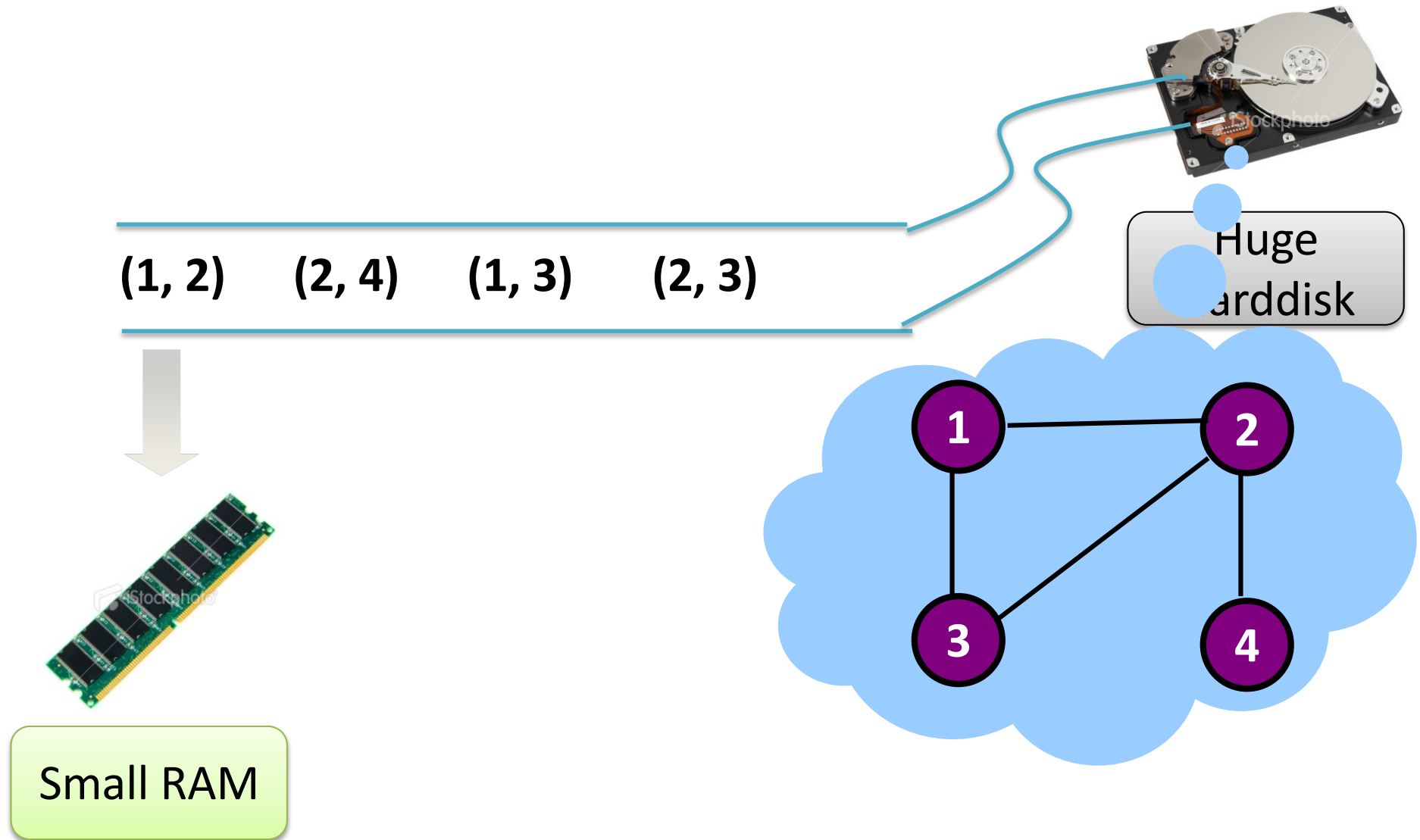
3 5 **9** 2 10 11 12 20



Small memory



# Graph Streaming model



# Applications

- Synchronization in distributed systems
- Network monitoring and traffic engineering
- Sensor networks, RFID tags
- Telecom call records
- Financial applications
- Web logs and click-streams
- Manufacturing processes
- Databases (Data Stream Management Systems)